

**In the Claims:**

1. (presently amended) A method of generating RSA cryptographic values, the method comprising the steps of:

Q2  
obtaining entity specific information (B) about a user;  
obtaining a first secret seed value ( $W_p$ ) and a second secret seed value ( $W_q$ );  
obtaining a third, publicly known, randomization value (IV) having a first portion ( $IV_p$ ) and a second portion ( $IV_q$ );  
dividing a potential range of RSA encryption values into a first interval and a second interval;  
generating a first initial value ( $XX_p$ ) based on the first secret seed value ( $W_p$ ), the second secret seed value ( $W_q$ ) and the first portion of the third randomization value ( $IV_p$ );  
mapping the first initial value to a entity specific segment of the first interval utilizing the obtained entity specific information (B) to provide a mapped first initial value ( $X_p$ );  
selecting a first user dependent RSA cryptographic value (p) from the entity specific segment of the first interval utilizing the mapped first initial value as a starting point for a search for the first user dependent RSA cryptographic value;  
generating a second initial value ( $XX_q$ ) based on the first user dependent RSA cryptographic value (p), the second secret seed value ( $W_q$ ) and the first portion of the third randomization value ( $IV_q$ );  
mapping the second initial value to a entity specific segment of the second interval utilizing the obtained entity specific information to provide a mapped second initial value ( $X_q$ ); and  
selecting a second user dependent RSA cryptographic value (q) from the entity specific segment of the second interval utilizing the mapped second initial value as a starting point for a search for the second user dependent RSA cryptographic value; and  
generating an RSA cryptographic key value for use in encrypting data utilizing the first and second user dependent RSA cryptographic values p and q.

2. (original) A method according to Claim 1, further comprising the step of generating auxiliary prime divisors corresponding to the first user dependent RSA cryptographic value (p) and the second user dependent RSA cryptographic value (q).

3. (original) A method according to Claim 2, wherein the auxiliary prime divisors are generated based upon the first secret seed value ( $W_p$ ), the second secret seed value ( $W_q$ ) and the third randomization value (IV).

4. (original) A method according to Claim 3, wherein  $p_0$  is a publicly known prime number whose length is at least  $n$  bits and  $g$  is a public generator, and wherein the step of generating auxiliary prime divisors comprises the steps of:

concatenating the first secret seed value ( $W_p$ ), the second secret seed value ( $W_q$ ) and the third randomization value (IV) so as to provide an exponent value ( $X$ );

determining an initial random value by determining  $Y = g^X \pmod{p_0}$ ;

selecting initial prime search values from the initial random value;

setting the most significant bit of the initial prime search values to "1" to provide final prime search values; and

selecting as the prime divisors the smallest prime value greater than or equal to the final prime search values.

5. (original) A method according to Claim 4, further comprising the steps of:

selecting at least one of a new first secret seed value ( $W_p$ ), a new second secret seed value ( $W_q$ ) and a new third randomization value (IV) if the length of at least one of the prime divisors is greater than the length of the final prime search values; and

re-generating the prime divisors if the length of at least one of the prime divisors is greater than the length of the final prime search values.

6. (original) A method according to Claim 4, wherein the initial prime search values have a first length if a public encryption exponent ( $e$ ) has an odd value and a second length of the public encryption exponent ( $e$ ) has an even value.

7. (original) A method according to Claim 5, wherein the first length is 120 bits and the second length is 118 bits.

8. (original) A method according to Claim 1, wherein the entity specific segments comprise the segments  $[A+(B(C-A))/2^b, A+((B+1)(C-A))/2^b]$  wherein  $A$  and  $C$  are the endpoints of the respective intervals and the entity specific information comprises  $b$  bits.

9. (original) A method according to Claim 8, wherein the RSA cryptographic values comprise  $n$  bits and wherein the first interval comprises RSA cryptographic values from the set of  $[\sqrt{2}(2^{n-1}), 2^{n-1} + 2^{n-3/2}]$  and the second interval comprises RSA cryptographic values from the set of  $[2^{n-1} + 2^{n-3/2}, 2^n]$ .

10. (presently amended) A method according to Claim 9, wherein the binary size of the RSA cryptographic values are  $2n$ , a size  $m$  is  $n-b-2$  and wherein the step of mapping the first initial value comprises the steps of:

linearly mapping the first initial value to a entity specific segment of the first interval utilizing the obtained entity specific information ( $B$ ) utilizing the linear mapping function

$$G_{1,U}(x) = 4(1 - \frac{1}{\sqrt{2}})x + \sqrt{2}2^{n-1} + 4(1 - \frac{1}{\sqrt{2}})(B-1)2^{m-1}; \text{ and}$$

selecting as the mapped first initial value ( $X_p$ ) the integer value which is not greater than the first initial value ( $XX_p$ ) mapped utilizing the mapping function  $G_{1,U}$ ; and

wherein the step of mapping the second initial value comprises the step of linearly mapping the second initial value to a entity specific segment of the second interval utilizing the obtained entity specific information ( $B$ ) utilizing the linear mapping function

$$G_{2,U}(x) = 4(1 - \frac{1}{\sqrt{2}})x + 2^{n-1} + 2^{n-3/2} + 4(1 - \frac{1}{\sqrt{2}})(B-1)2^{m-1}[[.]]; \text{ and}$$

selecting as the mapped second initial value ( $X_q$ ) the integer value which is not greater than the second initial value ( $XX_q$ ) mapped utilizing the mapping function  $G_{2,U}$ .

11. (original) A method according to Claim 1, wherein the entity specific information is biometric information.

12. (original) A method according to Claim 1, wherein the entity specific

information is a globally unique user identification.

13. (original) A method according to Claim 1, further comprising the steps of:

determining if a candidate for p is considered outside the range of RSA cryptographic values in the entity specific segment of the first interval;

selecting at least one of a new first secret seed value ( $W_p$ ), a new second secret seed value ( $W_q$ ) and a new third randomization value (IV) if a candidate for p is considered outside the range of RSA cryptographic values in the entity specific segment of the first interval;

determining if a candidate for q is considered outside the range of RSA cryptographic values in the entity specific segment of the second interval;

selecting at least one of a new first secret seed value ( $W_p$ ), a new second secret seed value ( $W_q$ ) and a new third randomization value (IV) if a candidate for q is considered outside the range of RSA cryptographic values in the entity specific segment of the second interval; and

restarting the cryptographic value generation utilizing the first and second secret seed values and third randomization value if either a candidate for p is considered outside the range of RSA cryptographic values in the entity specific segment of the first interval or if a candidate for q is considered outside the range of RSA cryptographic values in the entity specific segment of the second interval.

14. (original) A method according to Claim 1 further comprising the steps of:

determining if  $2^{16}-1$  candidates for p have been rejected in selecting the first user dependent RSA cryptographic value;

selecting at least one of a new first secret seed value ( $W_p$ ), a new second secret seed value ( $W_q$ ) and a new third randomization value (IV) if  $2^{16}-1$  candidates for p have been rejected in selecting the first user dependent RSA cryptographic value;

determining if  $2^{16}-1$  candidates for q have been rejected in selecting the second user dependent RSA cryptographic value;

selecting at least one of a new first secret seed value ( $W_p$ ), a new second secret seed

value ( $W_q$ ) and a new third randomization value (IV) if  $2^{16}-1$  candidates for  $q$  have been rejected in selecting the second user dependent RSA cryptographic value; and

restarting the cryptographic generation utilizing the first and second secret seed values and third randomization value if either  $2^{16}-1$  candidates for  $p$  have been rejected in selecting the first user dependent RSA cryptographic value or if  $2^{16}-1$  candidates for  $q$  have been rejected in selecting the second user dependent RSA cryptographic value.

02  
0074  
15. (original) A method according to Claim 1, wherein the step of generating a first initial value comprises the steps of:

mixing a concatenation of  $W_q$  and  $IV_q$  utilizing a publicly known mixing function;

concatenating  $W_p$  and  $IV_p$ ; and

EXCLUSIVE-ORing the mixed concatenation of  $W_q$  and  $IV_q$  and the concatenation  $W_p$  and  $IV_p$  to provide the first initial value ( $XX_p$ ); and

wherein the step of generating a second initial value comprises the steps of:

EXCLUSIVE ORing  $p$  and  $IV_p$ ;

mixing the EXCLUSIVE OR of  $p$  and  $IV_p$  utilizing the publicly known mixing function;

concatenating  $W_q$  and  $IV_q$ ; and

EXCLUSIVE-ORing the mixed EXCLUSIVE OR of  $p$  and  $IV_p$  and the concatenation of  $W_q$  and  $IV_q$  to provide the second initial value ( $XX_q$ ).

16. (original) A method according to Claim 1, further comprising the step of authenticating generated candidate RSA cryptographic values.

17. (presently amended) A method ~~according to Claim 16, wherein the step of authenticating an RSA cryptographic value comprising~~ comprises the steps of:

recovering two candidate prime values utilizing ~~the~~ a RSA public modulus ( $N$ ) and ~~the~~ a private signature exponent ( $d$ );

establishing a first of ~~the two~~ prime values as a first candidate cryptographic value ( $p'$ ) and the second of the two prime values as a second candidate cryptographic value ( $q'$ );

recovering first and second candidate seed values  $W_p'$  and  $W_q'$  from the first and

second candidate cryptographic values  $p'$  and  $q'$  and from the third publicly known seed value IV;

generating first and second RSA cryptographic values  $p''$  and  $q''$  utilizing  $W_p'$  and  $W_q'$  and IV; and

comparing  $p'$  and  $p''$  and  $q'$  and  $q''$  to authenticate the RSA cryptographic values.

18. (original) A method according to Claim 17, further comprising the step of determining that the RSA cryptographic values are not authentic if  $p'$  and  $q'$  are values outside the user defined segments of the first and second intervals.

19. (original) A method according to Claim 17, wherein the first of the two prime numbers is a smaller of the two prime numbers.

20. (original) A method according to Claim 17, wherein the step of recovering first and second candidate seed values  $W_p'$  and  $W_q'$  from the first and second candidate cryptographic values  $p'$  and  $q'$  and from the third publicly known seed value IV comprises the steps of:

inverse mapping the second candidate value  $q'$  to provide a first initial value  $S_q$ ;

EXCLUSIVE ORing the first candidate cryptographic value  $p'$  and  $IV_p$ ;

mixing the EXCLUSIVE OR of the first candidate cryptographic value  $p'$  and  $IV_p$  with the publicly known mixing function;

EXCLUSIVE ORing the mixed EXCLUSIVE OR of the first candidate cryptographic value  $p'$  and  $IV_p$  with  $IV_q$  to provide a first known value ( $N_q$ ) having a length ( $j$ );

determining if a value corresponding to the  $j$  least significant bits of  $S_q$  is less than the first known value  $N_q$ ;

EXCLUSIVE ORing the  $n-j$  most significant bits of the mixed concatenation of the first candidate cryptographic value  $p'$  and  $IV_p$  with the  $n-j$  most significant bits of  $S_q$  if the value corresponding to the  $j$  least significant bits of the first subsequent value is not less than the first known value  $N_q$ , to provide the second candidate seed value;

EXCLUSIVE ORing the  $n-j$  most significant bits of the mixed concatenation of the first candidate cryptographic value  $p'$  and  $IV_p$  with 1 subtracted from the value corresponding

to the  $n-j$  most significant bits of  $S_q$  if the value corresponding to the  $j$  least significant bits of the first subsequent value is less than the first known value  $N_q$ , to provide the second candidate seed value;

inverse mapping the first candidate value  $p'$  to provide a second initial value  $S_p$ ;

concatenating the second candidate seed value and  $IV_q$ ;

mixing the concatenation of the second candidate seed value and  $IV_q$  with the publicly known mixing function;

EXCLUSIVE ORing the mixed concatenation of the second candidate seed value and  $IV_q$  with  $IV_p$  to provide a second known value  $N_p$  having a length ( $j$ );

determining if a value corresponding to the  $j$  least significant bits of  $S_p$  is less than the second known value  $N_p$ ;

EXCLUSIVE ORing the  $n-j$  most significant bits of the mixed concatenation of the second candidate seed value and  $IV_q$  with the  $n-j$  most significant bits of  $S_p$  if value corresponding to the  $j$  least significant bits of the second subsequent value is not less than the second known value  $N_p$ , to provide the first candidate seed value;

EXCLUSIVE ORing the  $n-j$  most significant bits of the mixed concatenation of the second candidate seed value and  $IV_q$  with 1 subtracted from the value corresponding to the  $n-j$  most significant bits of  $S_p$  if the value corresponding to the  $j$  least significant bits of the second subsequent value is less than the second known value  $N_p$ , to provide the first candidate seed value.

21. (original) A method according to Claim 20, wherein  $j$  is 256 bits.

22. (presently amended) A system for generating an RSA cryptographic, utilizing entity specific information ( $B$ ) about a user, a first secret seed value ( $W_p$ ) and a second secret seed value ( $W_q$ ), and a third, publicly known, randomization value ( $IV$ ) having a first portion ( $IV_p$ ) and a second portion ( $IV_q$ ), comprising:

means for dividing a potential range of RSA encryption values into a first interval and a second interval;

means for generating a first initial value ( $XX_p$ ) based on the first secret seed value ( $W_p$ ), the second secret seed value ( $W_q$ ) and the first portion of the third randomization value ( $IV_p$ );

means for mapping the first initial value to a entity specific segment of the first interval utilizing the obtained entity specific information (B) to provide a mapped first initial value ( $X_p$ );

means for selecting a first user dependent RSA cryptographic value (p) from the entity specific segment of the first interval utilizing the mapped first initial value as a starting point for a search for the first user dependent RSA cryptographic value;

means for generating a second initial value ( $XX_q$ ) based on the first user dependent RSA cryptographic value (p), the second secret seed value ( $W_q$ ) and the first portion of the third randomization value ( $IV_q$ );

means for mapping the second initial value to a entity specific segment of the second interval utilizing the obtained entity specific information to provide a mapped second initial value ( $X_q$ ); and

means for selecting a second user dependent RSA cryptographic value (q) from the entity specific segment of the second interval utilizing the mapped second initial value as a starting point for a search for the second user dependent RSA cryptographic value; and

means for generating an RSA cryptographic key value for use in encrypting data utilizing the first and second user dependent RSA cryptographic values p and q.

23. (original) A system according to Claim 22, further comprising means for authenticating generated candidate RSA cryptographic values.

24. (presently amended) A system ~~according to Claim 23, wherein the means for authenticating comprises a message, comprising:~~

means for recovering two candidate prime values utilizing ~~the a~~ RSA public modulus (n) and ~~the a~~ private signature exponent (d) of the encrypted message;

means for establishing a first of ~~the two~~ prime values as a first candidate cryptographic value (p') and the second of the two prime values as a second candidate cryptographic value (q');



means for recovering first and second candidate seed values  $W_p'$  and  $W_q'$  from the first and second candidate cryptographic values  $p'$  and  $q'$  and from the third publicly known seed value IV;

means for generating first and second RSA cryptographic values  $p''$  and  $q''$  utilizing  $W_p'$  and  $W_q'$  and IV; and

means for comparing  $p'$  and  $p''$  and  $q'$  and  $q''$  to authenticate the message.

25. (original) A computer program product for generating an RSA cryptographic value, utilizing entity specific information (B) about a user, a first secret seed value ( $W_p$ ) and a second secret seed value ( $W_q$ ), and a third, publicly known, randomization value (IV) having a first portion ( $IV_p$ ) and a second portion ( $IV_q$ ), comprising:

a computer readable storage medium having computer readable program code embodied in said medium, said computer readable program code comprising:

computer readable code which divides a potential range of RSA encryption values into a first interval and a second interval;

computer readable code which generates a first initial value ( $XX_p$ ) based on the first secret seed value ( $W_p$ ), the second secret seed value ( $W_q$ ) and the first portion of the third randomization value ( $IV_p$ );

computer readable code which maps the first initial value to a entity specific segment of the first interval utilizing the obtained entity specific information (B) to provide a mapped first initial value ( $X_p$ );

computer readable code which selects a first user dependent RSA cryptographic value (p) from the entity specific segment of the first interval utilizing the mapped first initial value as a starting point for a search for the first user dependent RSA cryptographic value;

computer readable code which generates a second initial value ( $XX_q$ ) based on the first user dependent RSA cryptographic value (p), the second secret seed value ( $W_q$ ) and the first portion of the third randomization value ( $IV_q$ );

computer readable code which maps the second initial value to a entity specific segment of the second interval utilizing the obtained entity specific information to provide a mapped second initial value ( $X_q$ ); and

computer readable code which selects a second user dependent RSA cryptographic

value (q) from the entity specific segment of the second interval utilizing the mapped second initial value as a starting point for a search for the second user dependent RSA cryptographic value.

26. (original) A computer program product according to Claim 25, further comprising computer readable code which authenticates generated candidate RSA cryptographic values.

27. (presently amended) A computer program product ~~according to Claim 26,~~  
~~wherein the computer readable code which authenticates comprises:~~ for authenticating an  
RSA cryptographic value, comprising:

a computer readable storage medium having computer readable program code  
embodied in said medium, said computer readable program code comprising:

computer readable code which recovers two candidate prime values utilizing ~~the a~~  
RSA public modulus (n) and ~~the a~~ private signature exponent (d) of the encrypted message;

computer readable code which establishes a first of the two prime values as a first  
candidate cryptographic value (p') and the second of the two prime values as a second  
candidate cryptographic value (q');

computer readable code which recovers first and second candidate seed values  $W_{p'}$   
and  $W_{q'}$  from the first and second candidate cryptographic values p' and q' and from the third  
publicly known seed value IV;

computer readable code which generates first and second RSA cryptographic values  
p" and q" utilizing  $W_{p'}$  and  $W_{q'}$  and IV; and

computer readable code which compares p' and p" and q' and q" to authenticate the  
message.

28. (new) A system according to Claim 22, further comprising means for  
generating auxiliary prime divisors corresponding to the first user dependent RSA  
cryptographic value (p) and the second user dependent RSA cryptographic value (q).

29. (new) A system according to Claim 28, wherein the auxiliary prime divisors are generated based upon the first secret seed value ( $W_p$ ), the second secret seed value ( $W_q$ ) and the third randomization value (IV).

30. (new) A method according to Claim 29, wherein  $p_0$  is a publicly known prime number whose length is at least  $n$  bits and  $g$  is a public generator, and wherein the means for generating auxiliary prime divisors comprises:

means for concatenating the first secret seed value ( $W_p$ ), the second secret seed value ( $W_q$ ) and the third randomization value (IV) so as to provide an exponent value ( $X$ );

means for determining an initial random value by determining  $Y = g^X \pmod{p_0}$ ;

means for selecting initial prime search values from the initial random value;

means for setting the most significant bit of the initial prime search values to "1" to provide final prime search values; and

means for selecting as the prime divisors the smallest prime value greater than or equal to the final prime search values.

31. (new) A system according to Claim 30, further comprising:

means for selecting at least one of a new first secret seed value ( $W_p$ ), a new second secret seed value ( $W_q$ ) and a new third randomization value (IV) if the length of at least one of the prime divisors is greater than the length of the final prime search values; and

means for re-generating the prime divisors if the length of at least one of the prime divisors is greater than the length of the final prime search values.

32. (new) A system according to Claim 30, wherein the initial prime search values have a first length if a public encryption exponent ( $e$ ) has an odd value and a second length of the public encryption exponent ( $e$ ) has an even value.

33. (new) A system according to Claim 31, wherein the first length is 120 bits and the second length is 118 bits.

34. (new) A system according to Claim 22, wherein the entity specific segments comprise the segments  $[A+(B(C-A))/2^b, A+((B+1)(C-A))/2^b]$  wherein  $A$  and  $C$  are the endpoints of the respective intervals and the entity specific information comprises  $b$  bits.

35. (new) A method according to Claim 34, wherein the RSA cryptographic values comprise  $n$  bits and wherein the first interval comprises RSA cryptographic values from the set of  $[\sqrt{2}(2^{n-1}), 2^{n-1} + 2^{n-3/2}]$  and the second interval comprises RSA cryptographic values from the set of  $[2^{n-1} + 2^{n-3/2}, 2^n]$ .

36. (new) A system according to Claim 35, wherein the binary size of the RSA cryptographic values are  $2n$ , a size  $m$  is  $n-b-2$  and wherein the means for mapping the first initial value comprises:

means for linearly mapping the first initial value to a entity specific segment of the first interval utilizing the obtained entity specific information ( $B$ ) utilizing the linear mapping function  $G_{1,U}(x) = 4(1 - \frac{1}{\sqrt{2}})x + \sqrt{2} 2^{n-1} + 4(1 - \frac{1}{\sqrt{2}})(B-1)2^{m-1}$ ; and

means for selecting as the mapped first initial value ( $X_p$ ) the integer value which is not greater than the first initial value ( $XX_p$ ) mapped utilizing the mapping function  $G_{1,U}$ ; and

wherein the means for mapping the second initial value comprises means for linearly mapping the second initial value to a entity specific segment of the second interval utilizing the obtained entity specific information ( $B$ ) utilizing the linear mapping function

$G_{2,U}(x) = 4(1 - \frac{1}{\sqrt{2}})x + 2^{n-1} + 2^{n-3/2} + 4(1 - \frac{1}{\sqrt{2}})(B-1)2^{m-1}$ ; and

means for selecting as the mapped second initial value ( $X_q$ ) the integer value which is not greater than the second initial value ( $XX_q$ ) mapped utilizing the mapping function  $G_{2,U}$ .

37. (new) A system according to Claim 22, further comprising:

means for determining if a candidate for  $p$  is considered outside the range of RSA cryptographic values in the entity specific segment of the first interval;

means for selecting at least one of a new first secret seed value ( $W_p$ ), a new second secret seed value ( $W_q$ ) and a new third randomization value ( $IV$ ) if a candidate for  $p$  is

considered outside the range of RSA cryptographic values in the entity specific segment of the first interval;

means for determining if a candidate for  $q$  is considered outside the range of RSA cryptographic values in the entity specific segment of the second interval;

means for selecting at least one of a new first secret seed value ( $W_p$ ), a new second secret seed value ( $W_q$ ) and a new third randomization value (IV) if a candidate for  $q$  is considered outside the range of RSA cryptographic values in the entity specific segment of the second interval; and

means for restarting the cryptographic value generation utilizing the first and second secret seed values and third randomization value if either a candidate for  $p$  is considered outside the range of RSA cryptographic values in the entity specific segment of the first interval or if a candidate for  $q$  is considered outside the range of RSA cryptographic values in the entity specific segment of the second interval.

38. (new) A system according to Claim 22 further comprising:

means for determining if  $2^{16}-1$  candidates for  $p$  have been rejected in selecting the first user dependent RSA cryptographic value;

means for selecting at least one of a new first secret seed value ( $W_p$ ), a new second secret seed value ( $W_q$ ) and a new third randomization value (IV) if  $2^{16}-1$  candidates for  $p$  have been rejected in selecting the first user dependent RSA cryptographic value;

means for determining if  $2^{16}-1$  candidates for  $q$  have been rejected in selecting the second user dependent RSA cryptographic value;

means for selecting at least one of a new first secret seed value ( $W_p$ ), a new second secret seed value ( $W_q$ ) and a new third randomization value (IV) if  $2^{16}-1$  candidates for  $q$  have been rejected in selecting the second user dependent RSA cryptographic value; and

means for restarting the cryptographic generation utilizing the first and second secret seed values and third randomization value if either  $2^{16}-1$  candidates for  $p$  have been rejected in selecting the first user dependent RSA cryptographic value or if  $2^{16}-1$  candidates for  $q$  have been rejected in selecting the second user dependent RSA cryptographic value.

39. (new) A system according to Claim 22, wherein the means for generating a

first initial value comprises:

means for mixing a concatenation of  $W_q$  and  $IV_q$  utilizing a publicly known mixing function;

means for concatenating  $W_p$  and  $IV_p$ ; and

means for EXCLUSIVE-ORing the mixed concatenation of  $W_q$  and  $IV_q$  and the concatenation  $W_p$  and  $IV_p$  to provide the first initial value ( $XX_p$ ); and

wherein the means for generating a second initial value comprises:

means for EXCLUSIVE ORing  $p$  and  $IV_p$ ;

means for mixing the EXCLUSIVE OR of  $p$  and  $IV_p$  utilizing the publicly known mixing function;

means for concatenating  $W_q$  and  $IV_q$ ; and

means for EXCLUSIVE-ORing the mixed EXCLUSIVE OR of  $p$  and  $IV_p$  and the concatenation of  $W_q$  and  $IV_q$  to provide the second initial value ( $XX_q$ ).

40. (new) A system according to Claim 24, further comprising means for determining that the RSA cryptographic values are not authentic if  $p'$  and  $q'$  are values outside the user defined segments of the first and second intervals.

41. (new) A system according to Claim 24, wherein the first of the two prime numbers is a smaller of the two prime numbers.

42. (new) A system according to Claim 24 wherein the means for recovering first and second candidate seed values  $W_p'$  and  $W_q'$  from the first and second candidate cryptographic values  $p'$  and  $q'$  and from the third publicly known seed value  $IV$  comprises:

means for inverse mapping the second candidate value  $q'$  to provide a first initial value  $S_q$ ;

means for EXCLUSIVE ORing the first candidate cryptographic value  $p'$  and  $IV_p$ ;

means for mixing the EXCLUSIVE OR of the first candidate cryptographic value  $p'$  and  $IV_p$  with the publicly known mixing function;

means for EXCLUSIVE ORing the mixed EXCLUSIVE OR of the first candidate cryptographic value  $p'$  and  $IV_p$  with  $IV_q$  to provide a first known value ( $N_q$ ) having a length

(j);

means for determining if a value corresponding to the  $j$  least significant bits of  $S_q$  is less than the first known value  $N_q$ ;

means for EXCLUSIVE ORing the  $n-j$  most significant bits of the mixed concatenation of the first candidate cryptographic value  $p'$  and  $IV_p$  with the  $n-j$  most significant bits of  $S_q$  if the value corresponding to the  $j$  least significant bits of the first subsequent value is not less than the first known value  $N_q$ , to provide the second candidate seed value;

means for EXCLUSIVE ORing the  $n-j$  most significant bits of the mixed concatenation of the first candidate cryptographic value  $p'$  and  $IV_p$  with 1 subtracted from the value corresponding to the  $n-j$  most significant bits of  $S_q$  if the value corresponding to the  $j$  least significant bits of the first subsequent value is less than the first known value  $N_q$ , to provide the second candidate seed value;

means for inverse mapping the first candidate value  $p'$  to provide a second initial value  $S_p$ ;

means for concatenating the second candidate seed value and  $IV_q$ ;

means for mixing the concatenation of the second candidate seed value and  $IV_q$  with the publicly known mixing function;

means for EXCLUSIVE ORing the mixed concatenation of the second candidate seed value and  $IV_q$  with  $IV_p$  to provide a second known value  $N_p$  having a length  $(j)$ ;

means for determining if a value corresponding to the  $j$  least significant bits of  $S_p$  is less than the second known value  $N_p$ ;

means for EXCLUSIVE ORing the  $n-j$  most significant bits of the mixed concatenation of the second candidate seed value and  $IV_q$  with the  $n-j$  most significant bits of  $S_p$  if value corresponding to the  $j$  least significant bits of the second subsequent value is not less than the second known value  $N_p$ , to provide the first candidate seed value; and

means for EXCLUSIVE ORing the  $n-j$  most significant bits of the mixed concatenation of the second candidate seed value and  $IV_q$  with 1 subtracted from the value corresponding to the  $n-j$  most significant bits of  $S_p$  if the value corresponding to the  $j$  least significant bits of the second subsequent value is less than the second known value  $N_p$ , to provide the first candidate seed value.

43. (new) A computer program product according to Claim 25, further comprising computer program code which generates auxiliary prime divisors corresponding to the first user dependent RSA cryptographic value ( $p$ ) and the second user dependent RSA cryptographic value ( $q$ ).

44. (new) A computer program product according to Claim 43, wherein the auxiliary prime divisors are generated based upon the first secret seed value ( $W_p$ ), the second secret seed value ( $W_q$ ) and the third randomization value (IV).

45. (new) A computer program product according to Claim 44, wherein  $p_0$  is a publicly known prime number whose length is at least  $n$  bits and  $g$  is a public generator, and wherein the computer program code which generates auxiliary prime divisors comprises:

computer program code which concatenates the first secret seed value ( $W_p$ ), the second secret seed value ( $W_q$ ) and the third randomization value (IV) so as to provide an exponent value ( $X$ );

computer program code which determines an initial random value by determining  $Y = g^X \pmod{p_0}$ ;

computer program code which selects initial prime search values from the initial random value;

computer program code which sets the most significant bit of the initial prime search values to "1" to provide final prime search values; and

computer program code which selects as the prime divisors the smallest prime value greater than or equal to the final prime search values.

46. (new) A computer program product according to Claim 45, further comprising:

computer program code which selects at least one of a new first secret seed value ( $W_p$ ), a new second secret seed value ( $W_q$ ) and a new third randomization value (IV) if the length of at least one of the prime divisors is greater than the length of the final prime search values; and



computer program code which re-generates the prime divisors if the length of at least one of the prime divisors is greater than the length of the final prime search values.

47. (new) A computer program product according to Claim 45, wherein the initial prime search values have a first length if a public encryption exponent ( $e$ ) has an odd value and a second length if the public encryption exponent ( $e$ ) has an even value.

48. (new) A computer program product according to Claim 46, wherein the first length is 120 bits and the second length is 118 bits.

49. (new) A computer program product according to Claim 25, wherein the entity specific segments comprise the segments  $[A+(B(C-A))/2^b, A+((B+1)(C-A))/2^b]$  wherein  $A$  and  $C$  are the endpoints of the respective intervals and the entity specific information comprises  $b$  bits.

50. (new) A computer program product according to Claim 49, wherein the RSA cryptographic values comprise  $n$  bits and wherein the first interval comprises RSA cryptographic values from the set of  $[\sqrt{2}(2^{n-1}), 2^{n-1} + 2^{n-3/2}]$  and the second interval comprises RSA cryptographic values from the set of  $[2^{n-1} + 2^{n-3/2}, 2^n]$ .

51. (new) A computer program product according to Claim 50, wherein the binary size of the RSA cryptographic values are  $2n$ , a size  $m$  is  $n-b-2$  and wherein the computer program code which maps the first initial value comprises:

computer program code which linearly maps the first initial value to a entity specific segment of the first interval utilizing the obtained entity specific information ( $B$ ) utilizing the linear mapping function  $G_{1,U}(x) = 4(1 - \frac{1}{\sqrt{2}})x + \sqrt{2} 2^{n-1} + 4(1 - \frac{1}{\sqrt{2}})(B-1)2^{m-1}$ ; and

computer program code which selects as the mapped first initial value ( $X_p$ ) the integer value which is not greater than the first initial value ( $XX_p$ ) mapped utilizing the mapping function  $G_{1,U}$ ; and

wherein the computer program code which maps the second initial value comprises

computer program code which linearly maps the second initial value to a entity specific segment of the second interval utilizing the obtained entity specific information (B) utilizing the linear mapping function  $G_{2,U}(x) = 4(1 - \frac{1}{\sqrt{2}})x + 2^{n-1} + 2^{n-3/2} + 4(1 - \frac{1}{\sqrt{2}})(B-1)2^{m-1}$ ; and

computer program code which selects as the mapped second initial value ( $X_q$ ) the integer value which is not greater than the second initial value ( $XX_q$ ) mapped utilizing the mapping function  $G_{2,U}$ .

52. (new) A computer program product according to Claim 25, further comprising:

computer program code which determines if a candidate for p is considered outside the range of RSA cryptographic values in the entity specific segment of the first interval;

computer program code which selects at least one of a new first secret seed value ( $W_p$ ), a new second secret seed value ( $W_q$ ) and a new third randomization value (IV) if a candidate for p is considered outside the range of RSA cryptographic values in the entity specific segment of the first interval;

computer program code which determines if a candidate for q is considered outside the range of RSA cryptographic values in the entity specific segment of the second interval;

computer program code which selects at least one of a new first secret seed value ( $W_p$ ), a new second secret seed value ( $W_q$ ) and a new third randomization value (IV) if a candidate for q is considered outside the range of RSA cryptographic values in the entity specific segment of the second interval; and

computer program code which restarts the cryptographic value generation utilizing the first and second secret seed values and third randomization value if either a candidate for p is considered outside the range of RSA cryptographic values in the entity specific segment of the first interval or if a candidate for q is considered outside the range of RSA cryptographic values in the entity specific segment of the second interval.

53. (new) A computer program product according to Claim 25 further comprising:

computer program code which determines if  $2^{16}-1$  candidates for p have been rejected

in selecting the first user dependent RSA cryptographic value;

computer program code which selects at least one of a new first secret seed value ( $W_p$ ), a new second secret seed value ( $W_q$ ) and a new third randomization value (IV) if  $2^{16}-1$  candidates for p have been rejected in selecting the first user dependent RSA cryptographic value;

computer program code which determines if  $2^{16}-1$  candidates for q have been rejected in selecting the second user dependent RSA cryptographic value;

computer program code which selects at least one of a new first secret seed value ( $W_p$ ), a new second secret seed value ( $W_q$ ) and a new third randomization value (IV) if  $2^{16}-1$  candidates for q have been rejected in selecting the second user dependent RSA cryptographic value; and

computer program code which restarts the cryptographic generation utilizing the first and second secret seed values and third randomization value if either  $2^{16}-1$  candidates for p have been rejected in selecting the first user dependent RSA cryptographic value or if  $2^{16}-1$  candidates for q have been rejected in selecting the second user dependent RSA cryptographic value.

54. (new) A computer program product according to Claim 25, wherein the computer program code which generates a first initial value comprises:

computer program code which mixes a concatenation of  $W_q$  and  $IV_q$  utilizing a publicly known mixing function;

computer program code which concatenates  $W_p$  and  $IV_p$ ; and

computer program code which EXCLUSIVE-ORs the mixed concatenation of  $W_q$  and  $IV_q$  and the concatenation  $W_p$  and  $IV_p$  to provide the first initial value ( $XX_p$ ); and

wherein the computer program code which generates a second initial value comprises:

computer program code which EXCLUSIVE ORs p and  $IV_p$ ;

computer program code which mixes the EXCLUSIVE OR of p and  $IV_p$  utilizing the publicly known mixing function;

computer program code which concatenates  $W_q$  and  $IV_q$ ; and

computer program code which EXCLUSIVE-ORs the mixed EXCLUSIVE OR of p and  $IV_p$  and the concatenation of  $W_q$  and  $IV_q$  to provide the second initial value ( $XX_q$ ).

55. (new) A computer program product according to Claim 27, further comprising computer program code which determines that the RSA cryptographic values are not authentic if  $p'$  and  $q'$  are values outside the user defined segments of the first and second intervals.

56. (new) A computer program product according to Claim 27, wherein the first of the two prime numbers is a smaller of the two prime numbers.

57. (new) A computer program product according to Claim 27 wherein the computer program code which recovers first and second candidate seed values  $W_p'$  and  $W_q'$  from the first and second candidate cryptographic values  $p'$  and  $q'$  and from the third publicly known seed value IV comprises:

computer program code which inverse maps the second candidate value  $q'$  to provide a first initial value  $S_q$ ;

computer program code which EXCLUSIVE ORs the first candidate cryptographic value  $p'$  and  $IV_p$ ;

computer program code which mixes the EXCLUSIVE OR of the first candidate cryptographic value  $p'$  and  $IV_p$  with the publicly known mixing function;

computer program code which EXCLUSIVE ORs the mixed EXCLUSIVE OR of the first candidate cryptographic value  $p'$  and  $IV_p$  with  $IV_q$  to provide a first known value ( $N_q$ ) having a length ( $j$ );

computer program code which determines if a value corresponding to the  $j$  least significant bits of  $S_q$  is less than the first known value  $N_q$ ;

computer program code which EXCLUSIVE ORs the  $n-j$  most significant bits of the mixed concatenation of the first candidate cryptographic value  $p'$  and  $IV_p$  with the  $n-j$  most significant bits of  $S_q$  if the value corresponding to the  $j$  least significant bits of the first subsequent value is not less than the first known value  $N_q$ , to provide the second candidate seed value;

computer program code which EXCLUSIVE ORs the  $n-j$  most significant bits of the mixed concatenation of the first candidate cryptographic value  $p'$  and  $IV_p$  with 1 subtracted

from the value corresponding to the  $n-j$  most significant bits of  $S_q$  if the value corresponding to the  $j$  least significant bits of the first subsequent value is less than the first known value  $N_q$ , to provide the second candidate seed value;

computer program code which inverse maps the first candidate value  $p'$  to provide a second initial value  $S_p$ ;

computer program code which concatenates the second candidate seed value and  $IV_q$ ;

computer program code which mixes the concatenation of the second candidate seed value and  $IV_q$  with the publicly known mixing function;

computer program code which EXCLUSIVE ORs the mixed concatenation of the second candidate seed value and  $IV_q$  with  $IV_p$  to provide a second known value  $N_p$  having a length ( $j$ );

computer program code which determines if a value corresponding to the  $j$  least significant bits of  $S_p$  is less than the second known value  $N_p$ ;

computer program code which EXCLUSIVE ORs the  $n-j$  most significant bits of the mixed concatenation of the second candidate seed value and  $IV_q$  with the  $n-j$  most significant bits of  $S_p$  if value corresponding to the  $j$  least significant bits of the second subsequent value is not less than the second known value  $N_p$ , to provide the first candidate seed value; and

computer program code which EXCLUSIVE ORs the  $n-j$  most significant bits of the mixed concatenation of the second candidate seed value and  $IV_q$  with 1 subtracted from the value corresponding to the  $n-j$  most significant bits of  $S_p$  if the value corresponding to the  $j$  least significant bits of the second subsequent value is less than the second known value  $N_p$ , to provide the first candidate seed value.